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Probing transversity by measuring Λ polarisation in SIDIS



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ABSTRACT

Based on the observation of sizeable target-transverse-spin asymmetries in single-hadron and hadron-pair production in Semi-Inclusive measurements of Deep Inelastic Scattering (SIDIS), the chiral-odd transversity quark distribution functions h_1^q are nowadays well established. Several possible channels to access these functions were originally proposed. One candidate is the measurement of the polarisation of Λ hyperons produced in SIDIS off transversely polarised nucleons, where the transverse polarisation of the struck quark might be transferred to the final-state hyperon. In this article, we present the COMPASS results on the transversity-induced polarisation of Λ and $\bar{\Lambda}$ hyperons produced in SIDIS off transversely polarised protons. Within the experimental uncertainties, no significant deviation from zero was observed. The results are discussed in the context of different models taking into account previous experimental results on h_1^u and h_1^d .

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1. Introduction

The chiral-odd transversity quark distribution functions $h_1^q(x)$, hereafter referred to as transversity, were introduced as independent Parton Distribution Functions (PDFs) of the nucleon several decades ago [1–4]. Here, the superscript q denotes the quark flavour and x is the Bjorken variable. Several experimental approaches were proposed to access transversity in Semi-Inclusive measurements of Deep Inelastic Scattering (SIDIS) off transversely polarised nucleons.

Two of these approaches, the measurements of Collins asymmetries [5–8] and of azimuthal asymmetries of hadron pairs produced on transversely polarised protons [9–11], provided convincing evidence that transversity is indeed accessible experimentally. For u- and d-quarks, transversity was found to be different from zero at large x, where $h_1^u(x)$ and $h_1^d(x)$ are almost of the same size but opposite in sign, while $h_1^{\bar{u}}$ and $h_1^{\bar{d}}$ were found compatible with zero [12–16]. However, the uncertainties for the $d(\bar{d})$ -quark are about a factor of 3(2) larger than the uncertainties for the $u(\bar{u})$ -quark, due to the unbalance of the existing proton and deuteron data.

A third approach, independent from the previous two, is the SIDIS measurement of the polarisation of baryons produced in the process $\ell p^{\uparrow} \to \ell B^{\uparrow} X$, where ℓ denotes a lepton, p^{\uparrow} a transversely polarised target proton and B a baryon [2,17–19]. In the one-photon-exchange approximation, the hard interaction is $\gamma^* q^{\uparrow} \to q'^{\uparrow}$. When the virtual photon γ^* interacts with a transversely polarised quark q, the struck quark q' has a certain probability to transfer a fraction of the initial transverse polarisation to the final-state baryon. Thus a measurement of the polarisation of the final-

state baryon along the spin direction of the outgoing quark allows access to transversity [20,21].

Among all baryons, $\Lambda(\bar{\Lambda})$ hyperons are most suited to polarimetry studies due to their self-analysing weak decay into charged hadrons, $\Lambda \to p\pi^-$ ($\bar{\Lambda} \to \bar{p}\pi^+$), which occurs with a branching ratio BR = 63.9%. The polarisation $P_{\Lambda(\bar{\Lambda})}$ is accessible through the modulation of the angular distribution of the decay protons (antiprotons) [22]:

$$\frac{\mathrm{d}N_{\mathrm{p}(\bar{\mathrm{p}})}}{\mathrm{d}\cos\theta} \propto 1 + \alpha_{\Lambda(\bar{\Lambda})} P_{\Lambda(\bar{\Lambda})} \cos\theta \quad , \tag{1}$$

where θ is the proton (antiproton) emission angle with respect to the polarisation axis of the fragmenting quark in the $\Lambda(\bar{\Lambda})$ rest frame and $\alpha_{\Lambda(\bar{\Lambda})}$ is the weak decay constant. For the analysis presented in this paper, we use the most recent values of $\alpha_{\Lambda(\bar{\Lambda})}$ [23], i.e., $\alpha_{\Lambda}=0.750\pm0.009$ and $\alpha_{\bar{\Lambda}}=-0.758\pm0.010$.

As polarisation axis to access transversity we use the same that was used in QED calculations [24] for γ^* absorption. Accordingly, the components of the quark spins in initial (S_T) and final (S_T') state in the γ^* -nucleon system are connected by

$$S'_{T,x} = -D_{NN}S_{T,x}$$
 and $S'_{T,y} = D_{NN}S_{T,y}$, (2)

where as z-axis the virtual-photon direction is taken and as y-axis the normal to the lepton scattering (xz) plane (see Fig. 1). The virtual-photon depolarisation factor $D_{\rm NN}(y)=2(1-y)/(1+(1-y)^2)$ depends on y, the fraction of the initial lepton energy carried by the virtual photon in the target rest frame. The polarisation direction S_T' of the fragmenting quark is obtained as the reflection of the initial quark polarisation S_T with respect to the y-axis.

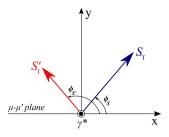


Fig. 1. Definition of the reference axes: The initial (S_T) and final (S_T') transverse quark spin-polarisation vectors are shown with respect to the μ - μ' scattering plane

In the collinear approximation, where the intrinsic transverse momentum of the struck quark is assumed to be negligible, and in the current fragmentation region the leading-order expression for the transversity-induced $\Lambda(\bar{\Lambda})$ polarisation integrated over the hadron transverse momentum $p_{\rm T}$ reads [20]:

$$\begin{split} P_{\Lambda(\bar{\Lambda})}(x,z,Q^{2}) &= \frac{\mathrm{d}\sigma^{\ell p^{\uparrow} \to \ell' \Lambda(\bar{\Lambda})^{\uparrow} X} - \mathrm{d}\sigma^{\ell p^{\uparrow} \to \ell' \Lambda(\bar{\Lambda})^{\downarrow} X}}{\mathrm{d}\sigma^{\ell p^{\uparrow} \to \ell' \Lambda(\bar{\Lambda})^{\uparrow} X} + \mathrm{d}\sigma^{\ell p^{\uparrow} \to \ell' \Lambda(\bar{\Lambda})^{\downarrow} X}} \\ &= f P_{T} D_{\text{NN}}(y) \frac{\sum_{q} e_{q}^{2} h_{1}^{q}(x,Q^{2}) H_{1,q}^{\Lambda(\bar{\Lambda})}(z,Q^{2})}{\sum_{q} e_{q}^{2} f_{1}^{q}(x,Q^{2}) D_{1,q}^{\Lambda(\bar{\Lambda})}(z,Q^{2})}. \end{split}$$

Here, Q^2 is the photon virtuality and z the fraction of the virtual photon energy carried by the $\Lambda(\bar{\Lambda})$ hyperon in the target rest frame; P_T is the target polarisation and f the target dilution factor representing the fraction of nucleons effectively polarised in the target. The sums in Eq. (3) run over all quark and antiquark flavours. The transversity distribution functions $h_1^q(x,Q^2)$ appear coupled to the chiral-odd fragmentation functions $H_{1,q}^{\Lambda(\bar{\Lambda})}(z,Q^2)$ that describe the spin transfer from the struck quark to the $\Lambda(\bar{\Lambda})$ hyperon:

$$H_{1,q}^{\Lambda(\bar{\Lambda})}(z,Q^2) = D_{1,q^{\uparrow}}^{\Lambda(\bar{\Lambda})^{\uparrow}}(z,Q^2) - D_{1,q^{\uparrow}}^{\Lambda(\bar{\Lambda})^{\downarrow}}(z,Q^2). \tag{4}$$

The up and down arrows indicate the polarisation directions for the $\Lambda(\bar{\Lambda})$ along the S_T' axis. The polarisation-independent fragmentation functions $D_{1,q}^{\Lambda(\bar{\Lambda})}(z,Q^2)$ are given by

$$D_{1,q}^{\Lambda(\bar{\Lambda})}(z,Q^{2}) = D_{1,q^{\uparrow}}^{\Lambda(\bar{\Lambda})^{\uparrow}}(z,Q^{2}) + D_{1,q^{\uparrow}}^{\Lambda(\bar{\Lambda})^{\downarrow}}(z,Q^{2}).$$
 (5)

Evidently, this approach gives access to transversity only if at least a part of the quark spin is transferred to the final state hadron, i.e. if $H_{1,q}^{\Lambda(\bar{\Lambda})}(z,Q^2) \neq 0$. Alternatively, once transversity is known, $P_{\Lambda(\bar{\Lambda})}$ can be used to shed light on the size of the transverse-spin-dependent quark fragmentation function.

The expression in Eq. (3) is valid at twist-2. In this work, we do not take into account higher-order terms [25], among which there is the one related to the spontaneous polarization [26]. As they are not oriented along the S_T' axis, their contribution is anyway expected to average to zero. Analogously, working -as said- in the collinear approximation, we refrain from considering possible k_T -related terms [27] dependent on the azimuthal angle ϕ of the $\Lambda(\bar{\Lambda})$ hyperon and on ϕ_S .

In general, $P_{\Lambda(\bar{\Lambda})}$ is not directly accessible from experimental data, as the detector acceptance distorts the angular distributions. Therefore, the measured angular distributions become

$$\frac{\mathrm{d}N_{\mathrm{p}(\bar{\mathrm{p}})}}{\mathrm{d}\cos\theta} \propto \left(1 + \alpha_{\Lambda(\bar{\Lambda})} P_{\Lambda(\bar{\Lambda})} \cos\theta\right) \cdot A(\theta),\tag{6}$$

where $A(\theta)$ is the detector acceptance depending on θ , which generally would have to be studied via detailed Monte Carlo simulations. However, in the COMPASS experiment [28] the specific target setup offers the unique opportunity to measure the transversity-induced polarisation avoiding acceptance corrections (see Sec. 3).

The analysis presented here was performed using the data collected by COMPASS in 2007 and 2010 with a 160 GeV/c longitudinally polarised muon beam from the CERN SPS and a transversely polarised NH3 target with proton polarisation $\langle P_T \rangle = 0.80$ and dilution factor $\langle f \rangle = 0.15$. In an earlier analysis, the $\Lambda(\bar{\Lambda})$ polarisation from the 2002-2004 data with a transversely polarised deuteron target [29] was found to be compatible with zero, as expected from the cancellation of u- and d-quark transversity (see Sec. 4.3). That measurement, however, suffered from limitations in statistical power and in spectrometer acceptance and from the lack of particle identification for a part of the data set. In this respect, the upcoming 2021/2022 run using a transversely polarised deuteron target [30] will be of great importance in drawing more definite conclusions.

2. Data selection and available statistics

In the data analysis, events are selected if they have at least one primary vertex, defined as the intersection point of a beam track. the scattered muon track, and other possible outgoing tracks. The primary vertex is required to be inside a target cell. The target consists of three cylindrical cells with 4 cm diameter, a central one of 60 cm and two outer ones of 30 cm length, each separated by 5 cm. Consecutive cells are polarised in opposite directions, so that data with both spin directions are recorded at the same time [7]. The extrapolated beam track is required to traverse all three target cells to ensure equal muon flux through the full target. Events originating from deep inelastic scattering are selected by requiring $Q^2 > 1$ (GeV/c)². For the invariant mass of the final state produced in the interaction of virtual-photon and nucleon, $W > 5 \text{ GeV}/c^2$ is required to avoid the region of exclusive resonance production. Furthermore the constraints 0.003 < x < 0.7 and 0.1 < y < 0.9 are applied. Here, the upper limit in x avoids a region of low statistics. and in y the limits avoid large radiative corrections and contamination from final-state pion decay (upper limit) and warrant a good determination of y (lower limit).

The Λ and $\bar{\Lambda}$ reconstruction is based on the detection of their decay products that originate from a decay vertex (V^0) downstream of the production vertex, which is not connected to the latter by charged tracks. Due to the long Λ lifetime, $\tau=(2.632\pm0.020)\cdot10^{-10}$ s, both vertices can be well separated. Exactly two oppositely charged hadrons with momentum larger than 1 GeV/c are required to originate from the decay vertex; the reconstructed momentum vector for such a hadron pair is required to be aligned with the vector linking the production and the decay vertices within a collinearity angle $\theta_{\rm coll} \leq 7$ mrad. In order to suppress background from photon conversion $\gamma \to e^+e^-$, the transverse momentum p_\perp of each hadron, calculated with respect to the line of flight of the hadron pair in its rest frame, has to be larger than 23 MeV/c.

Particle identification is performed using the RICH detector. In order to limit the ambiguity between $\Lambda(\bar{\Lambda})$ hyperons and K_s^0 mesons decaying into $\pi^+\pi^-$, it is necessary to ensure that the positive (negative) daughter particle is a proton (antiproton). However, a direct identification would drastically reduce the available

¹ Their contribution would not be negligible only in case of non-flat acceptance in $\cos \phi$ and $\cos 2\phi_S$. It has been checked that, for the data considered in this analysis, the acceptance in $\cos \phi$ is sufficiently flat, while compatible results can be found for positive and negative values of $\cos 2\phi_S$.

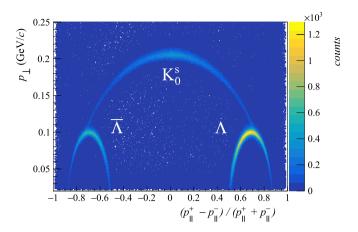
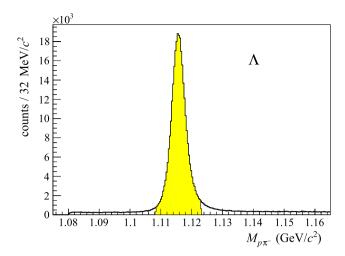


Fig. 2. Armenteros-Podolanski plot.

statistics due to the high Cherenkov threshold for protons of about 20 GeV/c for the radiator gas used (C_4F_{10}) . Therefore, assuming one charged track as negative (positive) pion, the corresponding positive (negative) track is considered to be a proton (antiproton) unless it is identified as positive (negative) electron, pion or kaon. The particle identification procedure is the same as it was used in previous analyses [31]. It is based on the calculation of the maximum likelihood \mathcal{L} for four mass hypotheses (e, K, π , p) and for the background, given the number of collected Cherenkov photons. In order to attribute a mass hypothesis M to a particle, \mathcal{L}_M is requested to be the highest and its ratio to the background hypothesis to be larger than an optimised threshold. This approach is applied to particles with momentum up to 50 GeV/c, a value at which pion/kaon separation becomes difficult. Beyond this limit, the highest likelihood is required not to be the one associated to the pion or kaon mass hypothesis.

The Armenteros-Podolanski plot [32,33] obtained after all aforementioned selection steps is shown in Fig. 2. The remaining K_s^0 contribution to the selected sample is visible as the symmetric arc, while a selection of the left and right halves of the figure allows to separate $\bar{\Lambda}$ (on the left) from Λ hyperons (on the right), based on the sign of the longitudinal momentum asymmetry $(p_{\parallel}^+ - p_{\parallel}^-)/(p_{\parallel}^+ + p_{\parallel}^-)$. Here, $p_{\parallel}^+(p_{\parallel}^-)$ indicates the longitudinal momentum of the positive (negative) decay particle in the hyperon rest frame with respect to the $\Lambda(\bar{\Lambda})$ line of flight. In Fig. 3 the Λ and $\bar{\Lambda}$ invariant mass spectra corresponding to these selections are shown. Here, only the K_s^0 in the crossing regions of the K_s^0 and $\Lambda(\bar{\Lambda})$ arcs contribute to the background. These invariant mass spectra are fitted with a superposition of a Gaussian function and a constant term using the PDG value for the Λ mass [34]. The background is evaluated with the sideband method considering two equally wide intervals on the left and on the right of the mass peak. Finally, hyperons are selected within a $\pm 3\sigma$ range from the peak, where $\sigma = 2.45 \text{ MeV}/c^2$ is obtained using all data shown in Fig. 3. Depending on the chosen kinematic bin, the signal-overbackground ratio ranges from 5.7 to 54.9. The total statistics after background subtraction are given in Table 1.

A significant fraction of Λ and $\bar{\Lambda}$ particles originates from the decay of heavier hyperons. Using the event generator LEPTO based on the Lund string model [35], tuned to reproduce the experimental distributions, 63% of the Λ and 68% of the $\bar{\Lambda}$ hyperons produced in the COMPASS kinematic regime are estimated to originate from direct string fragmentation [36]. These numbers get about 50% smaller when obtained with PYTHIA [37,38] or LEPTO with default tuning. The fractions of primary Λ and $\bar{\Lambda}$ hyperons, as obtained from the PYTHIA generator with default setting and excluding the feed-down contribution from weak decays, are given in Table 4 as a function of x, z and p_T in the current fragmen-



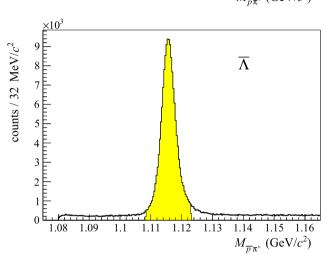


Fig. 3. Invariant mass spectra of Λ (top) and $\bar{\Lambda}$ (bottom) after all selection steps.

Table 1 Available statistics for Λ and $\bar{\Lambda}$ hyperons, after background subtraction, for years 2007 and 2010 and for their sum.

911 ± 227
$\frac{552 \pm 336}{4463 + 405}$
_

tation region. We have checked that the kinematic dependence of the fraction of directly produced Λ and $\bar{\Lambda}$ on $x,\,z$ and p_T is very small. In this analysis, the Λ and $\bar{\Lambda}$ hyperons coming from indirect production cannot be separated from those coming from direct production. Given all these uncertainties, their contribution is not taken into account as a systematic uncertainty, although it could dilute a possible polarisation signal.

3. Extraction method and results for $\Lambda(\bar{\Lambda})$ polarisation

For this analysis, as for all target spin asymmetries measured at COMPASS, systematic effects are minimised due to the unique target configuration described at the beginning of the previous section and to the fact that the data taking is divided into periods, each consisting of two subperiods in which data are taken with reversed polarisation orientation in each target cell.

As the transversity-induced $\Lambda(\bar{\Lambda})$ polarisation is to be measured along the spin direction of the fragmenting quark, this reference axis has to be determined on an event-by-event basis. The initial-quark spin is assumed to be aligned with the nucleon spin

and is thus vertical in the laboratory frame. Its transverse component is rotated by an azimuthal angle ϕ_S in the γ^* -nucleon system (Fig. 1). As described above, the spin direction of the quark after the interaction with the virtual photon is obtained by reflecting it with respect to the normal to the lepton scattering plane [21,24,39], $\phi_{S'} = \pi - \phi_S$. In the present analysis we determine the $\Lambda(\bar{\Lambda})$ polarisation along this direction.

The number of $\Lambda(\bar{\Lambda})$ hyperons emitting a proton (antiproton) in a given $\cos \theta$ range from a given target cell with a given direction of the target polarisation can be expressed as

$$\mathcal{N}_{\Lambda(\bar{\Lambda}),i}^{\{\prime\}}(\cos\theta) = \Phi_{i}^{\{\prime\}} \, \rho_{i}^{\{\prime\}} \, \bar{\sigma}_{\Lambda(\bar{\Lambda})}$$

$$\times (1_{\{-\}}^{+} \alpha_{\Lambda(\bar{\Lambda})} P_{\Lambda(\bar{\Lambda})} \cos(\theta + (i-1)\pi))$$

$$\times A_{i}^{\{\prime\}}(\cos\theta) \, .$$

$$(7)$$

Here, i = 1, 2 indicates the central or outer cells, respectively, $\Phi_i^{\{i\}}$ denotes the muon flux, $\rho_i^{\{\prime\}}$ the number of nucleons per unit area, and $\bar{\sigma}_{\Lambda(\bar{\Lambda})}$ is the cross section for the production of $\Lambda(\bar{\Lambda})$ hyperons. The acceptance term $A_i^{\{\prime\}}(\cos\theta)$ includes both geometrical acceptance, which is slightly different for each of the three target cells, and spectrometer efficiency. Primed quantities refer to data taken in subperiods after target polarisation reversal. After background subtraction, the four equations of Eq. (7) are combined to form a double ratio

$$\varepsilon_{\Lambda(\bar{\Lambda})}(\cos\theta) = \frac{\mathcal{N}_{\Lambda(\bar{\Lambda}),1}(\cos\theta)\mathcal{N}'_{\Lambda(\bar{\Lambda}),2}(\cos\theta)}{\mathcal{N}'_{\Lambda(\bar{\Lambda}),1}(\cos\theta)\mathcal{N}_{\Lambda(\bar{\Lambda}),2}(\cos\theta)} . \tag{8}$$

As described in Refs. [40,41], the acceptances cancel in this expression as long as in each $\cos \theta$ bin the acceptance ratios for the target cells after polarisation reversal are equal to those before, which is a reasonable assumption for the given setup. As described above, equal muon flux in all three target cells is maintained by the event selection, so that also the flux cancels in Eq. (8). For small values of the $\Lambda(\bar{\Lambda})$ polarisation it then becomes:

$$\varepsilon_{\Lambda(\bar{\Lambda})}(\cos\theta) \approx 1 + 4\alpha_{\Lambda(\bar{\Lambda})} P_{\Lambda(\bar{\Lambda})} \cos\theta.$$
 (9)

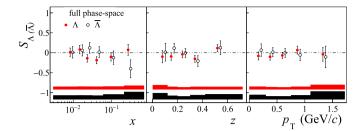
In each kinematic bin in x, z or p_T , the data sample is divided into eight $\cos\theta$ bins. This set of eight ε_j values is then fitted with the linear function $f=p_0(1+p_1\cos\theta)$, so that $P_{\Lambda(\bar{\Lambda})}$ is obtained as $P_{\Lambda(\bar{\Lambda})} = p_1/(4\alpha_{\Lambda(\bar{\Lambda})})$.

The transversity-induced polarisation is measured in the full phase-space and in the following regions:

- $z \ge 0.2$ and Feynman variable $x_F > 0$, our selection of the current fragmentation region;
- z < 0.2 or $x_F < 0$, complementary to the current fragmentation region;
- high $x: x \ge 0.032$;
- low x: x < 0.032;
- high p_T : p_T ≥ 0.5 GeV/c;
- low $p_{\rm T}$: $p_{\rm T} < 0.5 \; {\rm GeV}/c$.

In each of these regions, the data is scrutinised for possible systematic biases. The two main sources of systematic uncertainties are period compatibility and false $\Lambda(\bar{\Lambda})$ polarisations. The former are evaluated by comparing the results from the various periods of data taking, while the latter are evaluated by reshuffling the double ratio from Eq. (8) as $\frac{(\mathcal{N}_{\Lambda(\bar{\Lambda}),1}\mathcal{N}_{\Lambda(\bar{\Lambda}),2})}{(\mathcal{N}_{\Lambda(\bar{\Lambda}),1}^{\prime}\mathcal{N}_{\Lambda(\bar{\Lambda}),2})}$, so that transversity-induced $\Lambda(\bar{\Lambda})$ polarisations cancel. Effects of residual acceptance

variations are proven to be negligible by evaluating the K_s^0 po-



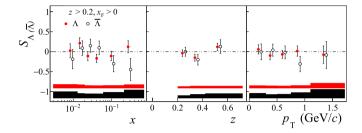


Fig. 4. Spin transfer $S_{\Lambda(\bar{\Lambda})}$ for the full phase-space (top) and for the current fragmentation region (bottom), as a function of x, z and p_T . The bands show the systematic uncertainties, while the error bars represent statistical uncertainties. The values in x, z and p_T are staggered for clarity.

larisation that is found to be compatible with zero as expected. In addition, $P_{\Lambda(\tilde{\Lambda})}$ is measured assuming the central cell split into two halves, thus creating two data samples by combining each half with one of the outer cells. Again, effects of acceptance variation are found to be negligible. A scale uncertainty of about 7.5% contributes to the overall systematics due to the uncertainty on the weak decay constant α (2%) and on the dilution and polarisation factors f and P_T (5% overall). In general, $\sigma_{\text{syst}} < 0.85 \sigma_{\text{stat}}$.

In Fig. 4, the results from the full phase-space and for the current fragmentation region are presented in terms of the spin

$$S_{\Lambda(\bar{\Lambda})} = \frac{P_{\Lambda(\bar{\Lambda})}}{f P_{T} D_{NN}(\gamma)},\tag{10}$$

by definition ranging from -1 to 1. The corresponding numerical values are given in the Appendix. The full set of data for all selections can be found on HEPData [42].

4. Interpretation of the results and predictions for future measurements

The polarisations shown in Fig. 4 are compatible with zero within the experimental uncertainties in all studied kinematic regions, which is in agreement with a recent measurement of the transverse spin transfer $D_{\rm TT}$ in polarised Drell-Yan [43]. From this result, applying different hypotheses, some conclusions will be drawn below on the size of the fragmentation function $H_{1}^{\Lambda}(z, Q^2)$ as well as on the strange quark transversity distribution $h_1^s(x, Q^2)$.

Following Eq. (3) and Eq. (10), in the current fragmentation region the spin transfer $S_{\Lambda(\bar{\Lambda})}$ reads

$$S_{\Lambda(\bar{\Lambda})} = \frac{\sum_{q} e_{q}^{2} h_{1}^{q} H_{1,q}^{\Lambda(\bar{\Lambda})}}{\sum_{q} e_{q}^{2} f_{1}^{q} D_{1,q}^{\Lambda(\bar{\Lambda})}},\tag{11}$$

where the dependences on x, z and Q^2 are omitted for simplicity.

4.1. Interpretation of the measured $\bar{\Lambda}$ polarisation

Considering the case of $\bar{\Lambda}$ hyperons, the favoured fragmentation functions $H_{1,\bar{u}}^{\bar{\Lambda}}$, $H_{1,\bar{d}}^{\bar{\Lambda}}$ and $H_{1,\bar{s}}^{\bar{\Lambda}}$ only appear in combination with the

sea-quarks \bar{u} , \bar{d} and \bar{s} . As $h_1^{\bar{s}}\approx 0$ can be assumed in analogy to $h_1^{\bar{u}}$ and $h_1^{\bar{d}}$, transversity is coupled only to unfavoured fragmentation functions. Here $H_{1,u}^{\bar{\Lambda}}$ and $H_{1,d}^{\bar{\Lambda}}$ dominate, as the s-quark contribution $h_1^s H_{1,s}^{\bar{\Lambda}}$ can be neglected because also h_1^s is expected to be small. This yields

$$\sum_{q} e_{q}^{2} h_{1}^{q} H_{1,q}^{\bar{\Lambda}} \propto 4 h_{1}^{u} H_{1,u}^{\bar{\Lambda}} + h_{1}^{d} H_{1,d}^{\bar{\Lambda}} \ . \tag{12}$$

The compatibility with zero of the measured polarisation for $\bar{\Lambda}$ hyperons is in agreement with expectations based on calculations for the ratios of favoured to unfavoured fragmentation functions (see, e.g., Ref. [44]). In these calculations, the unfavoured fragmentation functions are suppressed by a factor of about 4 to 5 in the current fragmentation region at z about 0.2 and rapidly decrease further for increasing z.

4.2. Interpretation of the measured Λ polarisation

Considering the case of Λ hyperons, one of the options suggested in e.g. Ref. [44] is to retain only the favoured combinations $(H_{1,u}^{\Lambda}, H_{1,d}^{\Lambda}, H_{1,s}^{\Lambda}, D_{1,u}^{\Lambda}, D_{1,d}^{\Lambda}, D_{1,s}^{\Lambda})$ in both numerator and denominator, resulting in:

$$S_{\Lambda} = \frac{4h_{1}^{u}H_{1,u}^{\Lambda} + h_{1}^{d}H_{1,d}^{\Lambda} + h_{1}^{s}H_{1,s}^{\Lambda}}{4f_{1}^{u}D_{1,u}^{\Lambda} + f_{1}^{d}D_{1,d}^{\Lambda} + f_{1}^{s}D_{1,s}^{\Lambda}}.$$
(13)

Isospin symmetry requires $D_{1,d}^{\Lambda}=D_{1,u}^{\Lambda}$ and $H_{1,d}^{\Lambda}=H_{1,u}^{\Lambda}$. For the s-quark fragmentation functions, it is often assumed that $D_{1,s}^{\Lambda}$ is proportional to $D_{1,u}^{\Lambda}$ with the proportionality constant r, which is the inverse of the strangeness suppression factor $\lambda=1/r$ [45,46]. In Ref. [47] its value is obtained from a fit of experimental baryon production data in e^+e^- annihilation to be $\lambda_{\Lambda}=1/r=0.44$. With these simplifications, Eq. (13) turns into

$$S_{\Lambda} = \frac{\left[4h_{1}^{u} + h_{1}^{d}\right]H_{1,u}^{\Lambda} + h_{1}^{s}H_{1,s}^{\Lambda}}{\left[4f_{1}^{u} + f_{1}^{d} + rf_{1}^{s}\right]D_{1,u}^{\Lambda}}.$$
(14)

The interpretation is now performed in three different scenarios. When needed, we use the CTEQ5D PDFs [48] for f_1^q , calculated at the x and Q^2 values of the data points, while the values of the transversity functions for u and d quarks are obtained from the fit presented in Ref. [12].

i) Transversity is non-zero only for valence quarks in the nucleon

If transversity is assumed non-vanishing only for valence quarks, h_1^s can be neglected and the expression for the spin transfer to the Λ further simplifies to:

$$S_{\Lambda} = \frac{[4h_1^u + h_1^d]H_{1,u}^{\Lambda}}{[4f_1^u + f_1^d + rf_1^s]D_{1,u}^{\Lambda}}.$$
 (15)

When S_{Λ} is now inspected only as a function of x, its dependence upon z, carried by the fragmentation functions, is integrated over. In a generic x bin centered at x^* it becomes

$$S_{\Lambda}|_{x=x^*} = \frac{\left[4h_1^u(x^*) + h_1^d(x^*)\right] \int_{0.2}^{1.0} dz H_{1,u}^{\Lambda}(z)}{\left[4f_1^u(x^*) + f_1^d(x^*) + rf_1^s(x^*)\right] \int_{0.2}^{1.0} dz D_{1,u}^{\Lambda}(z)}.$$
 (16)

Thus the measurement of S_{Λ} as a function of x can be used to extract, in each bin of x, the ratio \mathcal{R} of the z-integrated fragmentation functions $H_{1,u}^{\Lambda}$ and $D_{1,u}^{\Lambda}$:

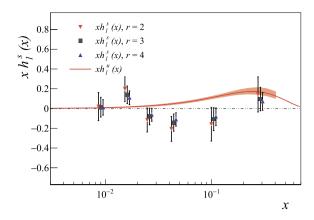


Fig. 5. Extracted values of $xh_1^s(x)$ for the three options r = 2, 3, 4. The u quark transversity curve from Ref. [12] is given for comparison. Only statistical uncertainties are shown and the x values are staggered for clarity.

$$\mathcal{R}(x^*) = \frac{\int_{0.2}^{1.0} dz H_{1,u}^{\Lambda}(z)}{\int_{0.2}^{1.0} dz D_{1,u}^{\Lambda}(z)} \bigg|_{x=x^*}$$

$$= \frac{4f_1^u(x^*) + f_1^d(x^*) + rf_1^s(x^*)}{4h_1^u(x^*) + h_1^d(x^*)} S_{\Lambda}|_{x=x^*}.$$
(17)

The mean value of \mathcal{R} over the measured x range is $\langle \mathcal{R} \rangle = -0.27 \pm 0.56$; it shows a weak dependence on r and is compatible with zero within the given statistics.

ii) Λ polarisation is carried by the s quark only

Assuming instead that the polarisation is entirely carried by the s-quark, as in the SU(3) non-relativistic quark model, $H_{1,u}^{\Lambda}$ can be neglected. Moreover, as suggested by Ref. [49], $H_{1,s}^{\Lambda}$ can be approximated with $D_{1,s}^{\Lambda}$ for z>0.2, yielding

$$S_{\Lambda} = \frac{h_1^s H_{1,s}^{\Lambda}}{\left[4f_1^u + f_1^d + rf_1^s\right] \frac{1}{r} D_{1,s}^{\Lambda}} \approx \frac{r h_1^s}{4f_1^u + f_1^d + rf_1^s},$$
 (18)

so that h_1^s can be extracted. In Fig. 5 the quantity $xh_1^s(x)$ is given for various choices of r and compared to the fitted value and accuracy of the $xh_1^u(x)$ distribution [12]. Again, only a weak dependence on r is observed. Although the data suggest a negative sign of $h_1^s(x)$, they are not precise enough to determine accurately $h_1^s(x)$ compared to the statistical precision of the $h_1^u(x)$ data.

iii) Polarised- Λ production is described by a quark-diquark fragmentation model

In the context of the quark-diquark model [49,50], the fragmentation of an unpolarised valence quark q into a final-state hadron is accompanied by the emission of a diquark D, which can be in a scalar (S) or vector (V) spin configuration. The probabilities $a_{\rm D}^{(q)}(z)$ associated to these two configurations are calculated in the model and enter the definition of the quark fragmentation function, which depends on z and on the masses of the fragmenting quark, the diquark and the produced hadron. Analogously, the fragmentation of a polarised quark is described through the probabilities $\hat{a}_{\rm D}^{(q)}(z)$. In the case of Λ production, the unpolarised fragmentation function of the s-quark, $D_{1,s}^{\Lambda}$, is taken as reference and used to express all the other fragmentation functions by introducing the flavour structure ratios $F_{\rm S}^{(u/s)}(z) = a_{\rm S}^{(u)}(z)/a_{\rm S}^{(s)}(z)$, $F_{\rm M}^{(u/s)}(z) = a_{\rm V}^{(u)}(z)/a_{\rm S}^{(s)}(z)$ and the spin-structure ratios $\hat{W}_{\rm D}^{q}(z) =$

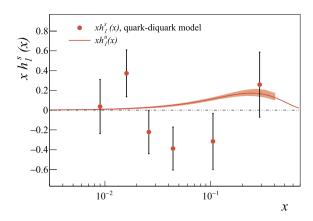


Fig. 6. Extracted values of $xh_1^5(x)$ according to a quark-diquark model [49,50]. The u-quark transversity curve from Ref. [12] is given for comparison. Only statistical uncertainties are shown.

 $\hat{a}_{\rm D}^{(q)}(z)/a_{\rm D}^{(q)}(z)$. The transversity-induced polarisation can thus be written as:

$$S_{\Lambda} = \frac{\left(4h_{1}^{u} + h_{1}^{d}\right) \cdot \frac{1}{4} \left[\hat{W}_{S}^{(u)} F_{S}^{(u/s)} - \hat{W}_{V}^{(u)} F_{M}^{(u/s)}\right] + h_{1}^{s} \hat{W}_{S}^{(s)}}{\left(4f_{1}^{u} + f_{1}^{d}\right) \cdot \frac{1}{4} \left[F_{S}^{(u/s)} + 3F_{M}^{(u/s)}\right] + f_{1}^{s}}, \quad (19)$$

where the x and z dependences are omitted for clarity. Information on h_1^s can be obtained by integrating Eq. (19) over z in each x bin. The values of $xh_1^s(x)$, as predicted by the quark-diquark model and based on the measured polarisation, are shown in Fig. 6. The dependence of the final results on the mass of the diquark (containing or not the s-quark) was found negligible.

Again, as in scenario ii), the data suggest a negative sign of $h_1^s(x)$, but statistical uncertainties are even larger in this case. Improved data will be needed to determine $h_1^s(x)$ more accurately.

4.3. Projections for future data taking with transversely polarised deuterons

The upcoming COMPASS run aims at collecting new precision SIDIS data using a polarised deuteron (^6LiD) target. The expected statistical uncertainties of the measured asymmetries are in the order of 60% of those estimated for the proton data. Compared to the existing deuteron data taken with the early COMPASS setup, we expect an accuracy improvement between a factor of two at small x and a factor of five at large x [30]. Some prospects for this measurement are described in the following.

The expression for the spin transfer, for Λ production on a transversely-polarised deuteron target, reads:

$$S_{\Lambda}^{D} = \frac{5(h_{1}^{u} + h_{1}^{d})H_{1,u}^{\Lambda} + 2h_{1}^{s}H_{1,s}^{\Lambda}}{5(f_{1}^{u} + f_{1}^{d})D_{1,u}^{\Lambda} + 2f_{1}^{s}D_{1,s}^{\Lambda}}.$$
(20)

It is already known from earlier COMPASS data that $h_1^d \approx -h_1^u$ [51,52]. The upcoming COMPASS run on a deuteron target will, in addition, allow us to measure with high precision the quantity $h_1^u + h_1^d$. Since the fragmentation function $H_{1,u}^{\Lambda}$ is expected to be smaller than the fragmentation function $H_{1,s}^{\Lambda}$, the numerator of Eq. (20) will be dominated by the product $h_1^s H_{1,s}^{\Lambda}$ if h_1^s is of significant size. Therefore, a new high statistics measurement of

the transversity-induced Λ polarisation on a deuteron target from the upcoming data is expected to be very sensitive to the product $h_1^s H_1^{\Lambda}$.

The measurements planned to access transversity on a 3 He target, expected in the future at SoLID [53], will also be important in order to better constrain the transversity for the s-quark and, in turn, the transversely polarised fragmentation functions $q \rightarrow \Lambda$.

5. Summary and outlook

Using a transversely polarised proton target and a 160 GeV/c muon beam, the transversity-induced polarisation along the spin axis of the struck quark was measured by COMPASS for Λ and $\bar{\Lambda}$ hyperons. While considered to be an excellent channel to access transversity, the results were found to be compatible with zero in all studied kinematic regions.

The statistical uncertainty on the measured polarisation is still large, despite the fact that all COMPASS data on a transversely polarised proton target were used, which are the only existing world data suitable for this measurement. Nevertheless, some information could be deduced from the existing data.

Under the hypothesis that transversity is non-vanishing only for valence quarks, the data were used to investigate the ratio of z-integrated polarised to unpolarised fragmentation functions. The results indicate a negative ratio, although compatible with zero due to the large uncertainties. If instead a non-relativistic SU(3) quark model or a quark-diquark model is considered, some information can be derived on the transversity distribution for the s quark. In both cases the results tend to support a negative s-quark transversity h_1^s within the large uncertainties given.

In addition, some prospects were given for measuring precisely the transversity-induced polarisation of Λ hyperons produced on a transversely polarised deuteron target. Since such a measurement is anticipated to be very sensitive to h_1^s , the results expected from the upcoming COMPASS run with a transversely polarised deuteron target in the years 2021 and 2022 will help to improve our knowledge on transversity.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A

Here, the spin transfer for Λ and $\bar{\Lambda}$ hyperons is given for the full phase-space (Table 2) and for the current fragmentation region (Table 3). For each bin the kinematic range is indicated, together with the mean values of x, Q^2 , z and p_T . These and other tables of results, for all the aforementioned kinematic regions, are available on HEPData. The fractions of primary Λ and $\bar{\Lambda}$ hyperons, as obtained from the PYTHIA generator with default setting, and excluding the feed-down contribution of weak decays, are given in Table 4.

Table 2 Spin transfer $S_{\Lambda(\bar{\Lambda})}$ from the full phase-space, as a function of x, z and p_T . For each kinematic bin the mean values of x, Q^2 , z and p_T are also given.

Full phase-space							
x range	$\langle x \rangle$	$\langle Q^2 \rangle (\text{GeV}/c)^2$	$\langle z \rangle$	$\langle p_{\rm T} \rangle \; ({\rm GeV}/c)$	S_{Λ}	$S_{ar{\Lambda}}$	
0.003 - 0.013	0.009	1.49	0.20	0.60	$0.014 \pm 0.106 \pm 0.074$	$0.014 \pm 0.145 \pm 0.107$	
0.013 - 0.020	0.016	2.06	0.25	0.59	$0.083\pm0.104\pm0.078$	$0.061 \pm 0.141 \pm 0.108$	
0.020 - 0.032	0.025	2.75	0.28	0.57	$-$ 0.138 \pm 0.096 \pm 0.077	$0.125\pm0.134\pm0.107$	
0.032 - 0.060	0.044	4.30	0.31	0.55	$-$ 0.186 \pm 0.089 \pm 0.076	$0.017 \pm 0.138 \pm 0.102$	
0.060 - 0.210	0.104	9.54	0.32	0.52	$-$ 0.101 \pm 0.105 \pm 0.080	$-$ 0.122 \pm 0.169 \pm 0.132	
0.210 - 0.700	0.290	26.5	0.34	0.53	$0.074 \pm 0.138 \pm 0.101$	$-$ 0.399 \pm 0.224 \pm 0.193	
z range	$\langle x \rangle$	$\langle Q^2 \rangle (\text{GeV}/c)^2$	$\langle z \rangle$	$\langle p_{\rm T} \rangle \; ({\rm GeV}/c)$	S_{Λ}	$S_{ar{\Lambda}}$	
0.00 - 0.12	0.023	4.15	0.09	0.55	$-$ 0.097 \pm 0.154 \pm 0.114	$0.015 \pm 0.222 \pm 0.163$	
0.12 - 0.20	0.031	4.14	0.16	0.57	$-$ 0.092 \pm 0.095 \pm 0.073	$0.117 \pm 0.123 \pm 0.099$	
0.20 - 0.30	0.041	4.13	0.25	0.57	$-\ 0.038 \pm 0.083 \pm 0.060$	$-$ 0.005 \pm 0.113 \pm 0.083	
0.30 - 0.42	0.050	4.11	0.35	0.56	$-$ 0.152 \pm 0.087 \pm 0.072	$-$ 0.205 \pm 0.136 \pm 0.114	
0.42 - 1.00	0.058	3.99	0.53	0.58	$0.118 \pm 0.090 \pm 0.071$	$0.127 \pm 0.173 \pm 0.136$	
p _T range	⟨ <i>x</i> ⟩	$\langle Q^2 \rangle (\text{GeV/}c)^2$	⟨ <i>z</i> ⟩	$\langle p_{\rm T} \rangle \; ({\rm GeV}/c)$	S_{Λ}	$S_{ar{\Lambda}}$	
0.00 - 0.30	0.045	4.33	0.27	0.19	$-0.079 \pm 0.101 \pm 0.076$	$0.066 \pm 0.158 \pm 0.120$	
0.30 - 0.50	0.042	4.20	0.26	0.40	$-$ 0.101 \pm 0.082 \pm 0.064	$0.016 \pm 0.114 \pm 0.085$	
0.50 - 0.75	0.039	4.02	0.26	0.62	$-$ 0.066 \pm 0.079 \pm 0.059	$-$ 0.002 \pm 0.115 \pm 0.084	
0.75 - 1.10	0.036	3.91	0.27	0.89	$0.068 \pm 0.099 \pm 0.074$	$-$ 0.054 \pm 0.145 \pm 0.110	
1.10 - 3.50	0.034	3.97	0.28	1.35	$-$ 0.039 \pm 0.172 \pm 0.122	- $0.104 \pm 0.271 \pm 0.206$	

Table 3 Spin transfer $S_{\Lambda(\bar{\Lambda})}$ from the current fragmentation region ($z \ge 0.2$, $x_F > 0$), as a function of x, z and p_T . For each kinematic bin the mean values of x, Q^2 , z and p_T are also given.

	Current fragmentation region							
x range	$\langle x \rangle$	$\langle Q^2 \rangle (\text{GeV}/c)^2$	⟨ <i>z</i> ⟩	$\langle p_{\rm T} \rangle \; ({\rm GeV}/c)$	S_{Λ}	${\mathcal S}_{ar\Lambda}$		
0.003 - 0.013	0.009	1.42	0.31	0.62	$0.024 \pm 0.174 \pm 0.104$	$-0.190 \pm 0.241 \pm 0.173$		
0.013 - 0.020	0.016	1.81	0.33	0.60	$0.212 \pm 0.136 \pm 0.096$	$0.088 \pm 0.184 \pm 0.128$		
0.020 - 0.032	0.026	2.31	0.35	0.57	$-$ 0.110 \pm 0.115 \pm 0.075	$0.148 \pm 0.164 \pm 0.119$		
0.032 - 0.060	0.044	3.60	0.37	0.54	$-0.169 \pm 0.103 \pm 0.073$	$0.096 \pm 0.169 \pm 0.119$		
0.060 - 0.210	0.105	8.19	0.38	0.51	$-0.110 \pm 0.118 \pm 0.077$	$-$ 0.303 \pm 0.203 \pm 0.156		
0.210 - 0.700	0.290	23.4	0.38	0.53	$0.122\pm0.152\pm0.098$	$-$ 0.448 \pm 0.276 \pm 0.215		
z range	$\langle x \rangle$	$\langle Q^2 \rangle (\text{GeV}/c)^2$	$\langle Z \rangle$	$\langle p_{\rm T} \rangle \; ({\rm GeV}/c)$	S_{Λ}	${\mathcal S}_{ar\Lambda}$		
0.20 - 0.30	0.040	4.12	0.25	0.57	$-0.039 \pm 0.083 \pm 0.052$	$-0.003 \pm 0.113 \pm 0.074$		
0.30 - 0.42	0.050	4.12	0.35	0.56	$-0.152 \pm 0.087 \pm 0.063$	$-$ 0.202 \pm 0.136 \pm 0.104		
0.42 - 1.00	0.058	3.99	0.53	0.58	$0.119 \pm 0.090 \pm 0.062$	$0.126\pm0.173\pm0.123$		
p _T range	$\langle x \rangle$	$\langle Q^2 \rangle (\text{GeV/}c)^2$	⟨ <i>Z</i> ⟩	$\langle p_{\rm T} \rangle \; ({\rm GeV}/c)$	S_{Λ}	$S_{ar{\Lambda}}$		
0.00 - 0.30	0.052	4.24	0.35	0.19	$0.056 \pm 0.117 \pm 0.073$	$-0.007 \pm 0.199 \pm 0.131$		
0.30 - 0.50	0.051	4.19	0.35	0.40	$-0.099 \pm 0.104 \pm 0.069$	$0.036 \pm 0.151 \pm 0.102$		
0.50 - 0.75	0.047	4.01	0.35	0.62	$-0.068 \pm 0.102 \pm 0.065$	$-0.021 \pm 0.163 \pm 0.109$		
0.75 - 1.10	0.043	3.89	0.36	0.89	$0.014 \pm 0.128 \pm 0.076$	$-$ 0.310 \pm 0.191 \pm 0.149		
1.10 - 3.50	0.039	3.99	0.36	1.36	$-$ 0.076 \pm 0.219 \pm 0.134	- 0.086 \pm 0.338 \pm 0.229		

Table 4 Fraction f^w of primary Λ and $\bar{\Lambda}$ hyperons according to the default PYTHIA generator, excluding the feed-down contribution of weak decays, as a function of x, z and p_T in the current fragmentation region.

	Fraction of primary Λ and $\bar{\Lambda}$ hyperons	
x range	f^w_Λ	$f^{w}_{ar{\Lambda}}$
0.003 - 0.013	0.45	0.45
0.013 - 0.020	0.45	0.46
0.020 - 0.032	0.46	0.50
0.032 - 0.060	0.43	0.51
0.060 - 0.210	0.41	0.46
0.210 - 0.700	0.36	0.46
z range	f^w_Λ	$f^{w}_{ar{\Lambda}}$
0.20 - 0.30	0.45	0.45
0.30 - 0.42	0.44	0.49
0.42 - 1.00	0.42	0.50
$p_{\rm T}$ range (GeV/ c)	f^w_Λ	$f^{w}_{ar{\Lambda}}$
0.00 - 0.30	0.40	0.43
0.30 - 0.50	0.41	0.46
0.50 - 0.75	0.44	0.50
0.75 - 1.10	0.50	0.53
1.10 - 3.50	0.53	0.62

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